Study Guide and Intervention

(continued)

Solving Quadratic Equations by Factoring

Solve Equations by Factoring When you use factoring to solve a quadratic equation, you use the following property.

Zero Product Property

For any real numbers a and b, if ab = 0, then either a = 0 or b = 0, or both a and b = 0.

Example

Solve each equation by factoring.

a.
$$3x^2 = 15x$$

$$3x^2 = 15x$$
 Original equation

$$3x^2 - 15x = 0$$
 Subtract 15x from both sides.

$$3x(x-5)=0$$
 Factor the binomial.

$$3x = 0$$
 or $x - 5 = 0$ Zero Product Property

$$x = 0$$
 or $x = 5$ Solve each equation.

The solution set is $\{0, 5\}$.

b.
$$4x^2 - 5x = 21$$

$$4x^2 - 5x = 21$$
 Original equation

$$4x^2 - 5x - 21 = 0$$
 Subtract 21 from both sides.

$$(4x + 7)(x - 3) = 0$$
 Factor the trinomial.

$$4x + 7 = 0$$
 or $x - 3 = 0$ Zero Product Property

$$x = -\frac{7}{4}$$
 or $x = 3$ Solve each equation.

The solution set is $\left\{-\frac{7}{4}, 3\right\}$.

Exercises

Solve each equation by factoring.

1.
$$6x^2 - 2x = 0$$

$$2. x^2 = 7x$$

$$3.20x^2 = -25x$$

4.
$$6x^2 = 7x$$

5.
$$6x^2 - 27x = 0$$

6.
$$12x^2 - 8x = 0$$

$$7.x^2 + x - 30 = 0$$

8.
$$2x^2 - x - 3 = 0$$

$$9. x^2 + 14x + 33 = 0$$

$$10.4x^2 + 27x - 7 = 0$$

11.
$$3x^2 + 29x - 10 = 0$$

12.
$$6x^2 - 5x - 4 = 0$$

13.
$$12x^2 - 8x + 1 = 0$$

$$14.\ 5x^2 + 28x - 12 = 0$$

15.
$$2x^2 - 250x + 5000 = 0$$

$$16.2x^2 - 11x - 40 = 0$$

17.
$$2x^2 + 21x - 11 = 0$$

$$18.\ 3x^2 + 2x - 21 = 0$$

$$19.8x^2 - 14x + 3 = 0$$

20.
$$6x^2 + 11x - 2 = 0$$

$$21.5x^2 + 17x - 12 = 0$$

$$22. 12x^2 + 25x + 12 = 0$$

$$23. 12x^2 + 18x + 6 = 0$$

$$24.7x^2 - 36x + 5 = 0$$